

**Project Title:****Crystal Structure Prediction and High-temperature Superconductivity of Li-RE-H System at High Pressures****Name:**

Yanming MA (1), Ryotaro ARITA (1), ○Toshiaki IITAKA (2)

**Laboratory at RIKEN:**(1) RIKEN Center for Emergent Matter Science, First-Principles Materials Science Research Team,  
(2) RIKEN Center for Computational Science, Discrete Event Simulation Research Team

1. Background and purpose of the project, relationship of the project with other projects

The search for room-temperature superconductivity has been a long-standing scientific endeavor ever since Heike Kamerlingh Onnes discovered in 1911 that mercury could conduct electricity without resistance below a critical temperature around 4 K. Twenty-four years after the discovery of this phenomenon known as superconductivity, Wigner and Huntington proposed that molecular hydrogen could undergo a phase transition into an atomic metallic hydrogen (AMH) phase at high pressures, which attracted great interest, especially after the conjecture of its ability to host very high-temperature superconductivity. Creating AMH, however, has proven extremely challenging due to the stringent synthesis and characterization conditions at very high pressures, currently recognized to be above 500 GPa. An early study found that hydrogen-rich metal hydride  $\text{Th}_4\text{H}_{15}$  was superconducting with a critical temperature  $T_c$  of 8 K at ambient pressure; later studies found that chemical substitution or doping could stabilize hydrogen-containing compounds that may host metallic and superconducting states approaching that of AMH. This line of work has been actively pursued after the conceptual development of using chemical precompression to facilitate the formation of hydrogen-dominant metallic alloys that host phonon-mediated high-temperature superconductivity.

Recent years have witnessed concerted efforts of exploring routes to achieving high- $T_c$  superconductivity in pressure-stabilized metal

hydrides (*e.g.*, refs 13–16). Following the theoretical predictions of stabilizing  $\text{H}_2\text{S}$  and  $\text{H}_3\text{S}$  at high pressures, a high  $T_c$  of 203 K at 150 GPa was documented experimentally. A different class of binary high- $T_c$  metal (M) hydrides based on clathrate structure having stoichiometry  $\text{MH}_6$  was predicted, led by the theoretical prediction on  $\text{CaH}_6$ . Further efforts to reach higher  $T_c$  led to the prediction and discovery of superhydrides with stoichiometries  $\text{MH}_n$  with  $n > 6$ . These efforts culminated in the experimental realization of superconducting  $\text{LaH}_{10}$  with a  $T_c$  of 250–260 K at pressures of 170–190 GPa, followed by  $\text{YH}_9$  with a  $T_c$  of 243 K at 201 GPa and  $\text{YH}_6$  with a  $T_c$  of 220 K at 166 or 237 GPa. Very recently, the long-missing clathrate structured  $\text{CaH}_6$  predicted in 2012 was successfully synthesized in the laboratory with a measured  $T_c$  of 215 K at 170 GPa. Other notable cases of clathrate structured high- $T_c$  hydrides include  $\text{YH}_{10}$ ,  $\text{Li}_2\text{MgH}_{16}$ , and  $\text{CaYH}_{12}$  from theory, and  $\text{ThH}_9$  and  $\text{ThH}_{10}$  from experiment.

An overriding idea underlying all of these efforts is to raise the hydrogen content while at the same time ensuring that the combination of compression chemical interactions are favorable to promote the  $\text{H}_2$  molecules in the dense structure to create material configurations closely resembling AMH in bonding environments. In this regard, a major task has thus been to find superhydrides with proper electron-rich heavy atoms that are capable of stabilizing hydrogen in a nonmolecular form to generate  $T_c$  exceeding that of the established superhydrides such as  $\text{LaH}_{10}$ .

Recent studies showed that rare-earth (RE) and actinide (An) elements are capable of maintaining

significant hydrogen by forming high-pressure clathrate compounds with a very high  $T_c$ . These results raise the exciting prospects of finding RE/An superhydrides containing even higher hydrogen content and hence further increased  $T_c$  that may approach or even exceed room temperature. Based on these considerations, we have explored electron-rich rare-earth and actinide elements that provide electrons to dissociate molecular hydrogen, thereby creating an AMH-like environment conducive to harboring high- $T_c$  superconductivity. Using our developed structural search algorithms, we uncovered a new class of hydrogen-superrich compounds with stoichiometry  $MH_{18}$  ( $M = \text{RE}$  or  $\text{An}$  atom). These extreme superhydrides exhibit unique  $H_{36}$  clathrate atomic cages with bonding environments similar to that predicted for AMH. First-principles calculations for different  $MH_{18}$  superhydrides predict diverse  $T_c$  values among the same stoichiometry that offer insights into the effect and nature of chemical precompression. Notable among these extreme superhydrides are  $\text{CeH}_{18}$  and  $\text{ThH}_{18}$  that exhibit above-room-temperature  $T_c$  near 330 K at 350 GPa and 321 K at 600 GPa, respectively, which represent the highest  $T_c$  values among all hitherto known thermodynamically stable superhydrides. The results of this study provide a wealth of information on material behaviors and key physics and chemistry insights that allow an in-depth study of the factors with major influence on achieving ultrahigh-temperature phonon-mediated superconductivity in hydrides, thereby opening a path for creating binary and multinary high- $T_c$  superhydrides that can operate at or even above room temperature.

Besides, a recent work claimed possible room-temperature superconductivity in the C–S–H system, but the structure and stoichiometry of the synthesized material remain unclear and require further investigation. we performed crystal structure searching of the C–S–H system at 300 GPa via our in-

house developed CALYPSO prediction methodology. A series of metastable crystals were identified with  $T_c$  values  $\sim 156$  K. The coordination number of the C and S atoms in compressed C–S–H crystals are four and six, respectively, with the formation of  $\text{CH}_4$  and  $\text{SH}_6$  molecules, and the remaining H atoms form  $\text{H}_2$  molecules in pairs. The formation of molecular crystals is the fundamental reason for such poor superconductivity. Besides, we searched for ground-state structures of C-doped  $Im\bar{3}m$ - $\text{H}_3\text{S}$  using the first-principles cluster expansion method. Superconductivity of  $\text{C}_x\text{S}_{1-x}\text{H}_3$  ( $x = 0.0625, 0.083, \text{ and } 0.10$ ) was estimated using primitive cells containing 40–64 atoms. The doping was found to lower the density of states at the Fermi level and then decrease the  $T_c$  values accordingly. Our results provide a comprehensive map between the crystal structure and superconductivity of carbonaceous sulfur hydride materials at high pressures, which might offer a valuable reference for further exploring the superconducting mechanism.

## 2. Specific usage status of the system and calculation method

During the fiscal year 2022, 3.6 million CPU hours were used to investigate hydrides with high superconductivity in all these two projects. We employ our developed swarm-intelligence-based CALYPSO structure prediction method, which is designed to search for the stable structures of given compounds, for the investigation of phase stability of C-S-H compounds at 300 GPa and RE-H compounds at 400 GPa. For most cases, the structure search for each chemical composition converges (evidenced by a lack of any additional structure with lower energy) after 1000~1200 structures were investigated. The energetic stability of different ternary stoichiometries is evaluated by their formation enthalpy of dissociated into the most competing element and binary compounds. The underlying energetic calculations are performed with the plane-

wave pseudopotential method as implemented in the VASP code. The Perdew-Burke-Ernzerhof generalized gradient approximation is chosen for the exchange-correlation functional. The phonon spectrum and electron-phonon coupling (EPC) of the stable compounds are calculated within the framework of linear response theory through the Quantum-ESPRESSO code, where ultrasoft pseudopotentials were used with a kinetic energy cutoff for wavefunctions of 80 Ry and a kinetic energy cutoff for charge density and potential of 1000 Ry. Electron-phonon couplings (EPC) constant  $\lambda$ ,  $\omega_{\log}$ , and  $T_c$  are solved using the elk code, as derived by the direct solution of the isotropic Migdal-Eliashberg equation.

### 3. Result

#### 3.1 Room-temperature superconductivity in compressed RE-H compounds

We performed structure searches in binary hydrides  $MH_m$  ( $m = 2-24$ ) over a wide range of hydrogen contents to predict stable structures, with a sharp focus on hydrogen-superrich phases. Particularly noteworthy was the finding of new stoichiometric Ce and Th extreme superhydrides Ce/ThH<sub>18</sub> stable at experimentally accessible pressures around 300 GPa after the zero-point energy (ZPE) was considered. Specifically, CeH<sub>18</sub> and ThH<sub>18</sub> become stable at reduced pressures of 315 and 281 GPa, respectively (see Figure 1a,b), making the experimental synthesis and characterization feasible. It is noted that these newly predicted extreme superhydrides possess higher  $T_c$  with competing synthesis pressure compared to the previously proposed high- $T_c$  binary superhydride YH<sub>10</sub>, which was not successfully synthesized in a recent experiment. A recent work reported that materials synthesis could be achieved near terapascal pressures, making it feasible to realize the materials predicted in this work. Further calculations for a broad range of RE and An hydride compounds up to 700 GPa reveal ubiquitous stability

of the MH<sub>18</sub> stoichiometry among diverse RE and An hydrides for RE/An = Y, La, Ce, Ac, and Th (Figure 1b). Details of the computational methods for the structure search and property calculations are provided in the Supporting Information.

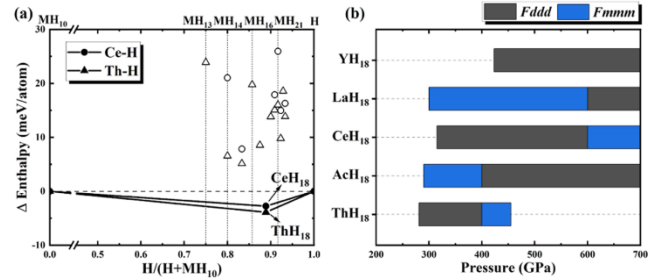


Figure 1. Calculated stability of predicted extreme superhydrides. (a) Calculated convex hull of newly identified extreme superhydrides CeH<sub>18</sub> and ThH<sub>18</sub>, both in the  $Fddd$  structure, calculated with respect to decomposition into Ce/ThH<sub>10</sub> and H<sub>2</sub> at 400 GPa. Data points located on the convex hull (solid lines) represent species stable against possible decomposition. The open symbols correspond to metastable/unstable compositions identified by the search process. (b) Stable pressure ranges of the predicted extreme superhydrides MH<sub>18</sub> with respect to decomposition into known MH<sub>x</sub> ( $x = 2, 4, 6, 9, 10, 12, 16,$  and  $17$ ) and  $Cmca$ -structured H<sub>2</sub>; zero-point energy (ZPE) was included in the calculations.

Conspicuous in the predicted crystal structure of the MH<sub>18</sub> extreme superhydrides is the H<sub>36</sub> clathrate cage, which contrasts with the H<sub>24</sub>, H<sub>29</sub>, and H<sub>32</sub> structural units found in previously identified hydrides with lower hydrogen contents. The peculiar three-dimensional hydrogen clathrate structure crystallizes in a unit cell with space group  $Fddd$  (Figure 2a) in which H<sub>36</sub> cages are linked by a 6H<sub>6</sub> ribbon-ring structure with two wrinkled H<sub>6</sub> hexagons above and below with bridge bonds connecting the H<sub>6</sub> hexagons to the 6H<sub>6</sub> ribbon ring (Figure 2b,c). At higher pressures, depending on the choice of the M atom, the H<sub>36</sub> clathrate units rearrange and stabilize in another structure with space group  $Fmmm$  (Figure 2b). Below we focus our analysis mainly on CeH<sub>18</sub> to showcase its prominent properties while also

discussing key data and trends involving other  $MH_{18}$  compounds.

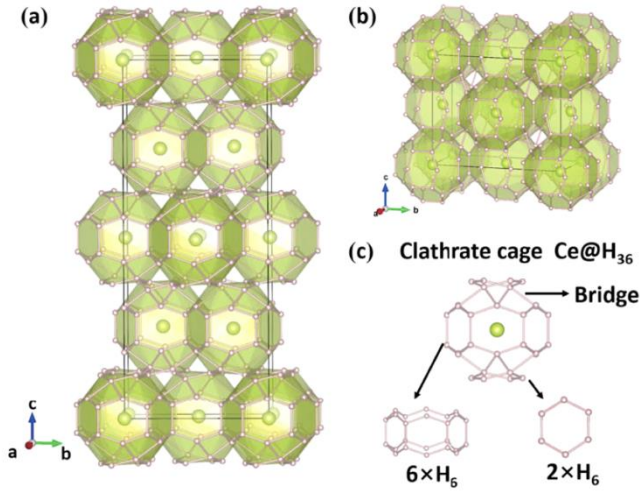


Figure 2. Crystal structure of  $MH_{18}$ . (a)  $Fddd$  and (b)  $Fmmm$  phase. (c) Building units of the  $M@H_{36}$  hydrogen clathrate cage, including a  $6H_6$  ribbon ring and two  $H_6$  hexagons, which are connected by pertinent bridge bonding networks. The large and small spheres represent the metal and hydrogen atoms, respectively.

We first examine the high-pressure electronic structure of  $CeH_{18}$ . The results clearly indicate the  $CeH_{18}$  phase is metallic with several bands crossing the Fermi level (Figure 3a, left), and hydrogen atoms make a substantial contribution to the electronic density of states (DOS) near the Fermi level, which is almost identical to the DOS contributed by the electrons from Ce (Figure 3a, right). The DOS is essentially flat around the Fermi energy, which is notably different from the DOS of  $LaH_{10}$ , which exhibits a van Hove singularity near the Fermi energy. The calculated band structures at different pressures reveal changes in band filling; notably, the hole-bands at the  $X$ -point, along the  $Z$ - $X$  path, and at the  $Y$ -point move down with increasing pressure, indicating a systematic pressure-driven electron transfer that suppresses  $T_c$  on further compression.

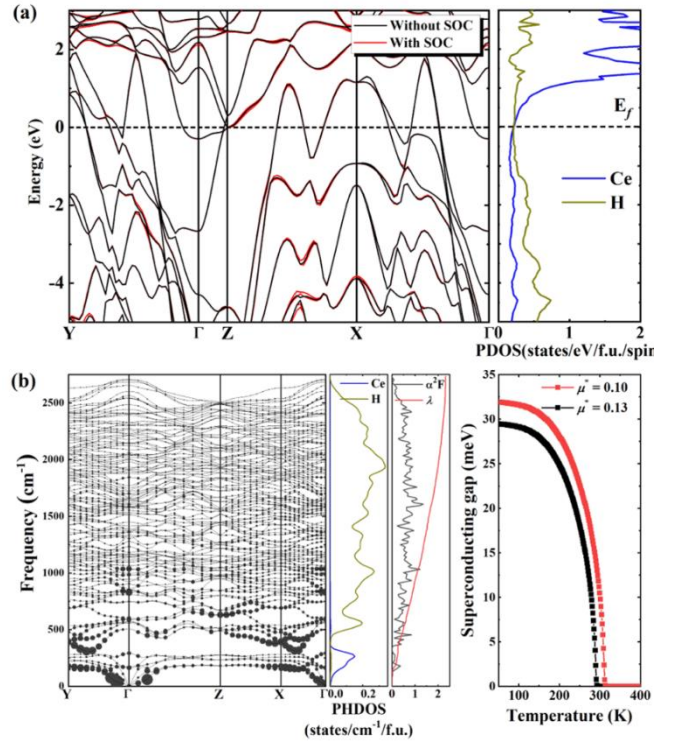


Figure 3. Electronic structures of  $CeH_{18}$ . (a) Electronic band structure (left) and projected density of states (right) of  $CeH_{18}$  at 400 GPa. The band structures without and with the inclusion of SOC are plotted with black and red lines, respectively. (b) Phonon dispersion curves with the strength of  $q$  resolved  $\lambda_q$  indicated by circle size (left), phonon density of states (PHDOS), Eliashberg spectral function  $a^2F(\omega)$  and EPC parameter  $\lambda(\omega)$  (middle), and superconducting energy gap (right) of  $CeH_{18}$  at 400 GPa.

Turning to the phonons and electron-phonon coupling in  $CeH_{18}$ , the calculated phonon dispersion results are shown in Figure 3b, left. No imaginary phonon modes are present in the entire Brillouin zone, indicating the dynamic stability of this crystal structure. We then computed the Eliashberg spectral function  $a^2F(\omega)$ , from which the electron-phonon coupling parameter can be obtained *via* a simple integration in the frequency domain. The resulting integrated electron-phonon coupling parameter  $\lambda = 2.3$  is quite large and comparable to that found for  $H_3S$  ( $\lambda = 2.2$ ). Such strong electron-phonon coupling makes various approximate weak-coupling  $T_c$  formulas generally unreliable, and an accurate description necessitates direct numerical solutions to

the Eliashberg equations. Adopting the latter method, we calculated superconducting energy gap and transition temperature and varied the Coulomb pseudopotential from  $\mu^* = 0.10$  (as is typically used) to  $\mu^* = 0.13$  to estimate a reasonable range of  $T_c$  values. The resulting  $T_c$  of 309–329 K (for  $\mu^* = 0.10$  and 0.13) at 350 GPa, where CeH<sub>18</sub> is stable, is well above the room temperature. These results are significantly higher than the highest  $T_c$  predicted for previously reported Ce superhydrides with lower hydrogen contents (*e.g.*,  $T_c = 117$  K for CeH<sub>9</sub>) and represent the highest predicted  $T_c$  among all known thermodynamically stable superhydrides.

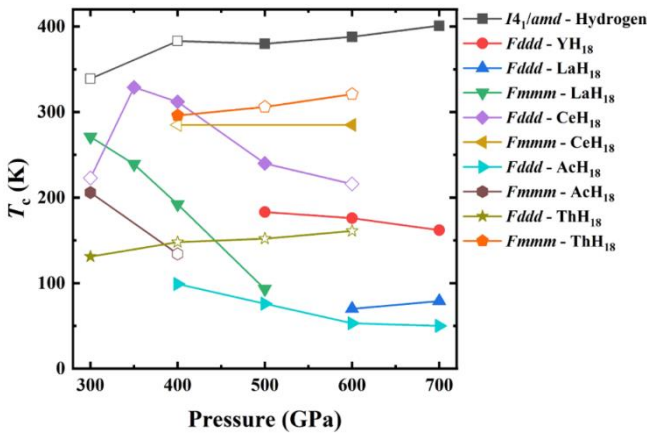


Figure 4. Superconducting critical temperatures of the predicted extreme superhydrides. Calculated  $T_c$  ( $\mu^* = 0.10$ ) for selected extreme superhydrides MH<sub>18</sub> compared with the results for the  $I_{41}/amd$  phase of solid hydrogen at high pressures. Solid (open) symbols represent the  $T_c$  data for stable (metastable) structural phases of the indicated MH<sub>18</sub> compounds and atomic metallic hydrogen.

To elucidate the underlying mechanisms for the predicted superconductivity of these extreme superhydrides, we calculated electronic, phonon, and electron–phonon coupling parameters, and the resulting critical temperatures using the Eliashberg equations of other selected MH<sub>18</sub> compounds. We also performed identical calculations for pure AMH in the  $I_{41}/amd$  structure, which is predicted to be stable or metastable in the same pressure range. First, we note that systematic examination of the energetics and dynamic stability of the MH<sub>18</sub> structures beyond their

stability fields reveal meta-stability to lower pressures of phases that maintain high superconducting temperatures (Figure 1b). The pressure dependence of  $T_c$  for the identified stable and metastable phases of MH<sub>18</sub> and  $I_{41}/amd$  hydrogen is given in Figure 4. The  $T_c$  values are distributed over a large range, from 50 K for  $Fddd$ -AcH<sub>18</sub> at 700 GPa up to near 330 K for  $Fddd$ -CeH<sub>18</sub> at 350 GPa ( $\mu^* = 0.10$ ). Moreover, the resulting critical temperatures vary considerably among the MH<sub>18</sub> superhydrides at the same pressure. The associated microscopic properties of each phase listed in Table 1 detail the differences in superconducting behavior among the compounds. The disparities within the same stoichiometry and clathrate structures stem from their characteristic vibrational frequencies, electron–phonon coupling parameters  $\lambda$ , and electronic DOS at the Fermi level  $\mathcal{N}(E_f)$ . We also have calculated the charge transfer for CeH<sub>18</sub> and LaH<sub>18</sub>, and the results show charge transfer from metal Ce/La to hydrogen atoms. The  $T_c$  values for different MH<sub>18</sub> structures may also be related to the different  $f$  electron fillings, *e.g.*, there are different  $T_c$  values for different MH<sub>10</sub> superhydrides as previously reported.

The present findings offer important clues for understanding the trends in superhydride  $T_c$  values that approach that of AMH at high pressures. Among the extreme superhydrides, CeH<sub>18</sub> exhibits the highest  $T_c$  over the entire pressure range, with nearest-neighbor H–H distances of 0.85–1.17 Å, close to that of  $I_{41}/amd$  structured AMH (1.0 Å) at 500 GPa. The calculated projected phonon DOS from the Ce and H atoms (Figure 3b) shows that the main contributions to the EPC come from the mid- and high-frequency hydrogen vibrations at 500–2500 cm<sup>-1</sup>. Further, most of MH<sub>18</sub> compounds exhibit monotonically decreasing  $T_c$  with increasing pressure, the exception being both  $Fddd$ - and  $Fmmm$ -ThH<sub>18</sub> for which  $T_c$  slightly increases on compression. The decrease in  $T_c$  with pressure of most superhydrides is reminiscent of the behavior of AMH at higher

pressures (700–1,000 GPa), which is consistent with the idea that chemical precompression in hydrogen compounds shifts their material behavior toward lower pressures. These insights are helpful for continued exploration and rational design of optimal superconducting superhydrides.

Table 1. Superconductivity of Predicted Structures<sup>a</sup>

compound	$P$	$\lambda$	$\omega_{\log}$	$N(E_F)$	$T_c$	$T_c(\text{SOC})$
H- $I4_1/amd$	300	2.34	1577	0.23	339(320)	
H- $I4_1/amd$	400	2.39	1719	0.25	383(362)	
H- $I4_1/amd$	500	2.24	1806	0.23	380(356)	
H- $I4_1/amd$	600	2.10	1953	0.23	388(362)	
H- $I4_1/amd$	700	2.08	2021	0.25	401(375)	
YH <sub>18</sub> - $Fddd$	500	1.50	1082	0.22	183(165)	
YH <sub>18</sub> - $Fddd$	600	1.28	1467	0.21	176(158)	
YH <sub>18</sub> - $Fddd$	700	1.10	1704	0.20	162(140)	
LaH <sub>18</sub> - $Fddd$	600	0.74	1638	0.16	70(55)	
LaH <sub>18</sub> - $Fddd$	700	0.78	1642	0.17	79(64)	
LaH <sub>18</sub> - $Fmmm$	300	2.46	1156	0.25	271(255)	
LaH <sub>18</sub> - $Fmmm$	350	1.68	1491	0.23	239(222)	
LaH <sub>18</sub> - $Fmmm$	400	1.28	1649	0.22	192(174)	
LaH <sub>18</sub> - $Fmmm$	500	0.82	1663	0.17	93(76)	
CeH <sub>18</sub> - $Fddd$	300	2.03	985	0.27	223(207)	224(208)
CeH <sub>18</sub> - $Fddd$	350	2.80	919	0.32	329(309)	330(310)
CeH <sub>18</sub> - $Fddd$	400	2.32	1294	0.33	312(292)	310(290)
CeH <sub>18</sub> - $Fddd$	500	1.85	920	0.27	240(212)	
CeH <sub>18</sub> - $Fddd$	600	1.64	844	0.26	216(194)	
CeH <sub>18</sub> - $Fmmm$	400	2.21	1260	0.22	285(265)	
CeH <sub>18</sub> - $Fmmm$	600	1.76	1388	0.22	285(262)	
AcH <sub>18</sub> - $Fddd$	400	0.92	1411	0.18	99(83)	
AcH <sub>18</sub> - $Fddd$	500	0.80	1480	0.17	76(62)	
AcH <sub>18</sub> - $Fddd$	600	0.65	1718	0.17	53(40)	
AcH <sub>18</sub> - $Fddd$	700	0.62	1844	0.18	50(37)	
AcH <sub>18</sub> - $Fmmm$	300	1.68	1217	0.23	206(190)	
AcH <sub>18</sub> - $Fmmm$	400	1.36	904	0.20	134(119)	
ThH <sub>18</sub> - $Fddd$	300	1.15	1227	0.21	131(116)	
ThH <sub>18</sub> - $Fmmm$	400	3.39	568	0.37	296(277)	296(277)
ThH <sub>18</sub> - $Fmmm$	500	1.92	1573	0.40	306(284)	306(285)
ThH <sub>18</sub> - $Fmmm$	600	2.13	1331	0.42	321(299)	321(299)

<sup>a</sup>Calculated pressure ( $P$  (GPa)) variation of  $\lambda$ ,  $\omega_{\log}$  (K),  $N(E_F)$  (states/Ry/atom/spin) and  $T_c$  (K) for  $\mu^* = 0.10(0.13)$  for selected MH<sub>18</sub> compounds in  $Fmmm$  or  $Fddd$  phase and hydrogen in the  $I4_1/amd$  structure.

We consider additional effects such as spin-orbit coupling (SOC), magnetism, and electron correlation that may affect the estimated  $T_c$  of the predicted MH<sub>18</sub> compounds. We take the highest  $T_c$  extreme superhydrides CeH<sub>18</sub> and ThH<sub>18</sub> as examples to assess these effects. Our calculations reveal that the  $T_c$  values are insensitive to SOC (Table 1), which is consistent with the nearly identical band structures

calculated with and without the SOC (Figure 3a). We examined the energetics of the magnetic structures of the predicted MH<sub>18</sub> compounds by considering six possible magnetic configurations (one ferromagnetic and five antiferromagnetic configurations). The results show that the nonmagnetic state is the most stable among all of the predicted MH<sub>18</sub> compounds. A recent work quantified the correlation between the  $f$  orbital states at the Fermi energy with  $T_c$  for the lanthanide hydrides. These results offer insights into the reason for CeH<sub>18</sub> and ThH<sub>18</sub> hosting high  $T_c$  values due to the fact that both Ce and Th elements have less partially filled  $f$  electron states. Although we have not considered electron correlation effects on the EPC due to a lack of available computational tools, we note that previous studies have shown that the experimental results on several hydrides and superhydrides (*e.g.*, those of La, Y, Th, and Ca) are well described by the theoretical results obtained within the current EPC computation scheme without considering the electron correlation effects. On this basis, it is expected that the results in the present work offer a reasonably accurate description of the superconductivity in the newly predicted MH<sub>18</sub> compounds. For other RE/An hydrides that are not discussed in this work, especially those with more filled  $f$  electron states, it is expected that the magnetic, SOC, and strong correlation effects play more prominent roles, and other hydrogen-rich superconducting hydrides cannot be ruled out. However, phononmediated superconductivity is unlikely to be the underlying mechanism in these systems, and related studies are beyond the scope of this work.

### 3.2 High-temperature superconductivity in C-S-H compound at 300 GPa

Based on the results from the variable-composition crystal structure searches and the cluster expansion, we constructed the ternary phase diagram of C–S–H as presented in Fig. 1(a). Unfortunately, no

thermodynamically stable C–S–H compounds were found, indicating all the ternary compounds tend to decompose into elements and binaries under certain conditions. Nevertheless, in previous high-throughput material discovery studies, the convention for the threshold between metastable (likely to be synthesized) and unstable (unlikely to be synthesized) compounds is 50 meV/atom. The same convention was adopted in this work. Therefore, metastable C–S–H compounds cannot be precluded from experimental synthesis.

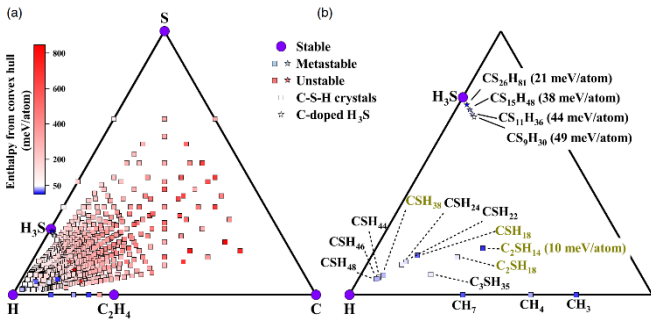


FIG. 1. (a) Calculated stabilities of  $C_xS_yH_z$  relative to C, S, H, and binary compounds at 300 GPa. H-rich molecular crystals and  $H_3S$ -like structures with low levels of carbon doping are presented with squares and stars, respectively. A square (or star) filling with blue or red indicates that the corresponding ternary compound is metastable or unstable. Purple circles indicate stable phases. (b) Metastable C–S–H compounds with formation enthalpies below 50 meV/atom at 300 GPa. Labels in gold or black indicate the corresponding ternary compounds are insulated or metallic.

We found that C–S–H compounds with high-H content or a low level of carbon doping are more stable than other compositions. Specifically, there are ten H-rich ternaries and four low-level C-doping compounds that are metastable with formation enthalpies lower than 50 meV/atom at 300 GPa [as shown in Fig. 1(b), formation enthalpies and structural parameters of these metastable compounds are listed in Table S1]. Among of which  $P\bar{3}$ - $C_2SH_{14}$  has the lowest enthalpy of decomposition at 300 GPa [10 meV/atom above the convex hull, as shown in Fig. 1(b)]. Further pressure may help to

reduce the formation enthalpy and stabilize the new compound, calculated formation enthalpy as a function of pressure is thus shown in Fig. S1, which shows that  $P\bar{3}$ - $C_2SH_{14}$  is not a thermodynamically stable structure at a wide range of pressures (200–400 GPa), and has the lowest enthalpy value of thermal decomposition of 6 meV/atom at 270 GPa. Then we focus on the crystal structures and superconductivity of the H-rich compounds.

TABLE I. Space group (S.G.), formation enthalpy ( $\Delta E$ , meV/atom), band gap (gap, eV), electronic density of states at the Fermi level [ $N(E_f)$ , states/spin/Ry/f.u.],  $\lambda$ ,  $\omega_{log}$  (K), and  $T_c$  (K) estimated using  $\mu^* = 0.10(0.13)$  for metastable C–S–H molecular crystals at 300 GPa [(M) indicates metallic phase].

Compound	S.G.	$\Delta E$	Gap	$N(E_f)$	$\lambda$	$\omega_{log}$	$T_c$
$C_2SH_{14}$	$P\bar{3}$	10	1.65				
$CSH_{18}$	$Cm$	18	0.21				
$CSH_{46}$ (M)	$P1$	32		4.62	0.97	1293	93(80)
$CSH_{48}$ (M)	$P1$	35		7.58	1.56	1071	156(142)
$CSH_{38}$	$P1$	36	0.27				
$CSH_{22}$ (M)	$P1$	44		2.64	0.99	1045	78(68)
$C_2SH_{18}$	$P\bar{1}$	45	0.79				
$C_3SH_{35}$ (M)	$P1$	46		6.59	2.47	558	156(143)
$CSH_{24}$ (M)	$P1$	47		4.34	2.09	595	138(125)
$CSH_{44}$ (M)	$P1$	50		5.51	1.50	791	113(100)

These metastable H-rich C–S–H compounds are all molecule crystals composed of  $CH_4$ ,  $SH_6$ , and  $H_2$  units. C atoms form  $CH_4$  molecule with neighboring H atoms. The valence electron configuration of the S atom is  $3s^23p^4$ , which makes it not surprising that the coordination number of S is six at 300 GPa, and then results in  $SH_6$  molecule units. Other H atoms form  $H_2$  molecules in pairs. Such molecule crystals are usually insulators and hard to be good conductors though insulation-metal phase transition may occur under high pressure. Calculations show that  $C_2SH_{14}$ ,  $CSH_{18}$ ,  $CSH_{38}$ , and  $C_2SH_{18}$  exhibit nonmetallic characteristics at 300 GPa with band gaps of 1.65, 0.21, 0.27, and 0.79 eV, respectively, while the other six metastable molecular crystals are metallic with  $T_c$  156 K (as shown in Table I). We discuss the structures and superconductivity of the most stable

$C_2SH_{14}$  and the highest superconducting  $CSH_{48}$  as representatives of H-rich molecular crystals.

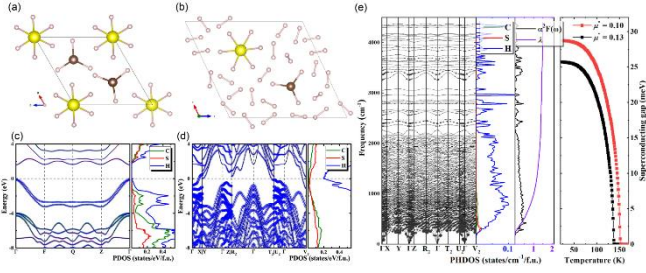


FIG. 2. Crystal structures of (a)  $P3-C_2SH_{14}$  and (b)  $P1-CSH_{48}$  at 300 GPa. The large, medium, and small spheres represent the S, C, and H atoms, respectively.  $CH_4$ ,  $SH_6$ , and  $H_2$  molecules are building units that form these two molecule crystals. Electronic band structure (left panel) and projected density of states (right panel) of (c)  $P3-C_2SH_{14}$  and (d)  $P1-CSH_{48}$  at 300 GPa. © Phonon dispersion curves with the strength of  $q$ -resolved  $\lambda_q$  indicated by circle size, projected phonon densities of states (PHDOS), isotropic Eliashberg spectral function  $\alpha^2F(\omega)$  and EPC parameter  $\lambda(\omega)$ , and superconducting gap of  $P1-CSH_{48}$  at 300 GPa.

Crystal structures of  $P3-C_2SH_{14}$  and  $P1-CSH_{48}$  are shown in Figs. 2(a) and 2(b), where the characteristics of molecular crystals are so obvious that they can be written as  $(CH_4)_2(SH_6)$  and  $(CH_4)(SH_6)(H_2)_{19}$ , respectively. To clarify the origin of metallic properties in  $P1-CSH_{48}$ , electron band structures and the project electronic density of states (PDOS) of insulating  $P3-C_2SH_{14}$  and metallic  $P1-CSH_{48}$  at 300 GPa is shown in Figs. 2(c) and 2(d). Calculated results show that  $CH_4$  and  $SH_6$  contribute more to the deep orbitals with lower energy due to there are strong covalent bonding behavior in C–H and S–H bonds, while hydrogen atoms make a substantial contribution to the electronic density of states near the Fermi level [ $\mathcal{N}(E_f)$ ], indicating that the existence of a large number of  $H_2$  units in the  $P1-CSH_{48}$  compound results in its metallic property. EPC calculations show an integrated electron-phonon coupling parameter  $\lambda$  of 1.56 at 300 GPa, which is not very large compared with the value of  $\lambda = 2.2$  for  $H_3S$ .

90% of the contribution to  $\lambda$  is derived from the–H–H vibration modes of  $250\text{--}2200\text{ cm}^{-1}$  [as shown in Fig. 2(e)].  $T_c$  values of the  $H_2$ -rich hydrides, such as  $MgH_{16}$  and  $YH_{24}$ , usually not higher than that of the molecular hydrogen ( $T_c$  of  $\approx 242\text{ K}$  at 450 GPa). Similarly, with a direct numerical solution to the Eliashberg equations,  $T_c$  of  $P1-CSH_{48}$  is estimated to be 142–156 K at 300 GPa, where the Coulomb pseudopotential was set to be the typical values of  $\mu^* = 0.10\text{--}0.13$ . Table shows a positive correlation between  $\lambda$ ,  $\mathcal{N}(E_f)$ , and the hydrogen content of C–S–H molecular crystals, which is consistent with the fact that the metallic and superconductivity of C–S–H molecular crystals are mainly due to the contribution of  $H_2$  molecules. Naturally,  $P1-CSH_{48}$ , with the highest hydrogen content, has the highest  $\mathcal{N}(E_f)$  and thus the highest  $T_c$  value (156 K) among the six metallic molecular crystals listed in Table I.

Next, we investigated the four metastable  $H_3S$ -like compounds with 3.7%, 6.25%, 8.3%, and 10% doped carbon, respectively, which were identified using the cluster expansion method. Primitive cells of these four  $H_3S$ -like compounds can be seen as supercells of the  $Im\bar{3}m-H_3S$  where sulfur atoms were replaced by carbon atoms. Thus, carbon atoms here are octahedrally coordinated by six hydrogen atoms (as shown in Fig. 3). Low-level carbon-doping localizes electrons in C–H bonds and reduced symmetry, which is detrimental to high-temperature superconductivity. To investigate how different levels of carbon doping affect the stability, electronic structure, and superconductivity of C–S–H compounds, detailed analysis were carried out on the  $Pm\bar{3}m-H_3S_{0.9375}C_{0.0625}$  ( $CS_{15}H_{48}$ ),  $C2/m-H_3S_{0.917}C_{0.083}$  ( $CS_{11}H_{36}$ ), and  $C2/m-H_3S_{0.9}C_{0.1}$  ( $CS_9H_{30}$ ) stoichiometries, since the electron-phonon coupling simulations of  $Im\bar{3}m-H_3S_{0.963}C_{0.037}$  ( $CS_{26}H_{81}$ ) exceed the limits of our current computing facilities. All of these three compounds are dynamically stable at 300 GPa and can be dynamically stable at pressures down to 260, 230, and 180 GPa, respectively (see Fig. S2 for



detail).

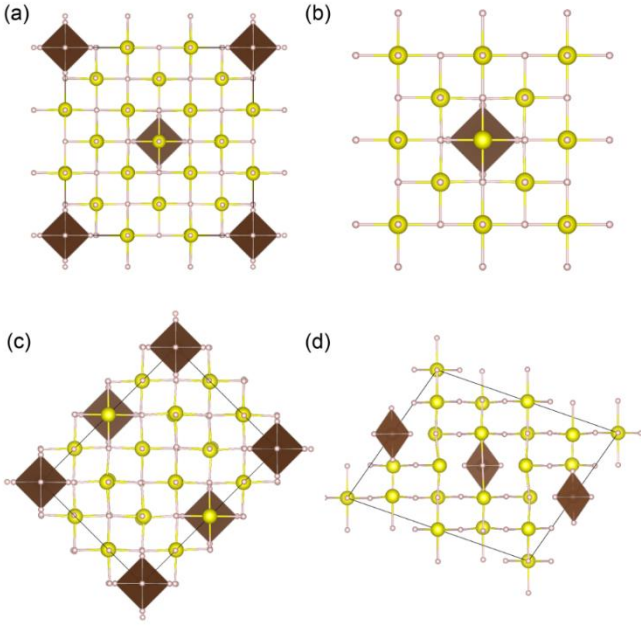


FIG. 3. Crystal structures of (a)  $Im\bar{3}m$ - $H_3S_{0.963}C_{0.037}$  ( $CS_{26}H_{81}$ ), (b)  $Pm\bar{3}m$ - $H_3S_{0.9375}C_{0.0625}$  ( $CS_{15}H_{48}$ ), (c)  $C2/m$ - $H_3S_{0.917}C_{0.083}$  ( $CS_{11}H_{36}$ ), and (d)  $C2/m$ - $H_3S_{0.9}C_{0.1}$  ( $CS_9H_{30}$ ) at 300 GPa. The large, medium, and small spheres represent the S, C, and H atoms, respectively. The translucent regular tetrahedrons represent the  $SH_6$ -like  $CH_6$  units.

Calculated superconductivity of compressed  $CS_{15}H_{48}$ ,  $CS_{11}H_{36}$ , and  $CS_9H_{30}$  is listed in Table II. To better visualize how doping affect superconductivity,  $N(E_f)$ ,  $\lambda$ , and  $T_c$  (K) for C-doped  $H_3S$  compounds with different doping ratios at 300 GPa are shown in Fig. 4(a). With the increase of C-doping concentration,  $T_c$  rises first and then decreases.  $CS_{11}H_{36}$  with a C-doped concentration of 8.3% has the highest  $T_c$  value. It is worth noting that, with the increase of doping concentration,  $T_c$  shows exactly the same trend as  $N(E_f)$ , which indicated that doping affects the  $N(E_f)$  thus  $T_c$  values. Additionally, the superconducting temperature increases with decreasing pressure [as shown in Fig. 4(b)], and  $CS_{11}H_{36}$  have the  $T_c$  value of 216 K at 230 GPa. Notably, the  $T_c$  values of C-doped  $H_3S$  compounds are lower than that of  $H_3S$  in the pressure range studied and are  $\approx 100$  K lower than the maximum measured value for the C-S-H superconductor, which is inconsistent with previous

studies.

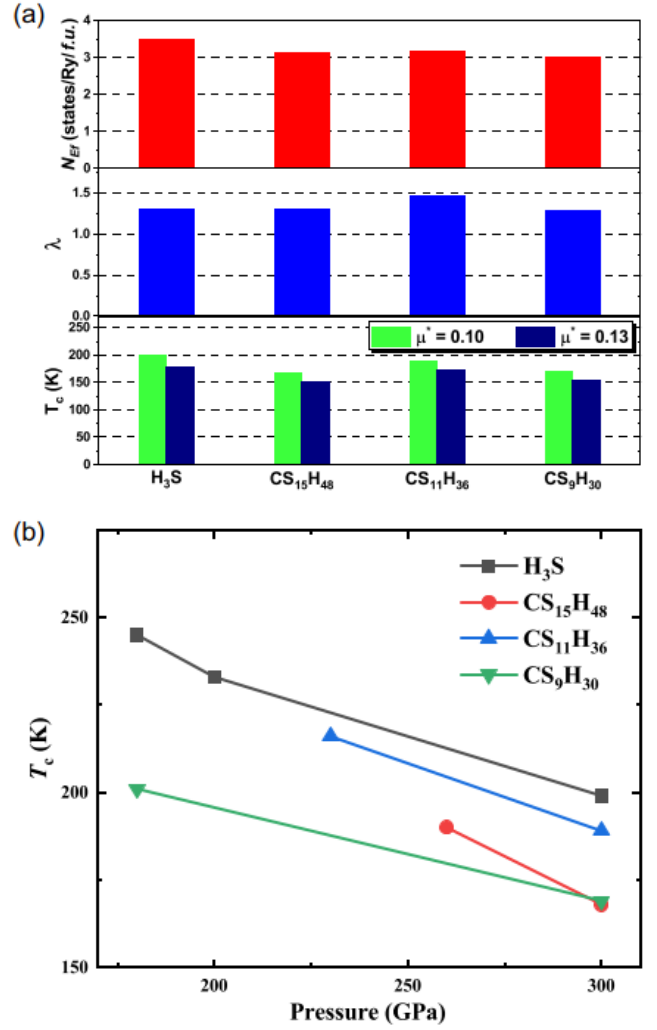


FIG. 4. (a) Calculated electronic density of states at the Fermi level [ $N(E_f)$ ] (top panel), the electron-phonon coupling parameter ( $\lambda$ ) (middle panel), and  $T_c$  (bottom panel) of  $H_3S$  and  $H_3S$ -like low level C-doping C-S-H compounds at 300 GPa. (b) Pressure dependence of  $T_c$  of  $H_3S$  and  $H_3S$ -like low level C-doping C-S-H compounds.

TABLE II. Primitive cells, space group (S.G.), pressure (GPa), electronic density of states at the Fermi level [ $N(E_f)$ , states/spin/Ry/f.u.],  $\lambda$ ,  $\omega_{log}$  (K), isotropic superconducting gap (meV) at 40 K, and  $T_c$  (K) estimated using  $\mu^* = 0.10(0.13)$  for  $H_3S$  and  $H_3S$ -like low-level C-doping C-S-H compounds.

Compound	Primitive cell	S.G.	Pressure	$N(E_f)$	$\lambda$	$\omega_{log}$	$\Delta$	$T_c$
$H_3S$	$H_3S$	$Im\bar{3}m$	180	3.20	2.35	1134	51.32	245(230)
$H_3S$	$H_3S$	$Im\bar{3}m$	200	3.31	1.83	1366	45.68	233(217)
$H_3S$	$H_3S$	$Im\bar{3}m$	300	3.48	1.30	1679	35.26	199(178)
$H_3S_{0.9375}C_{0.0625}$	$CS_{15}H_{48}$	$Pm\bar{3}m$	260	3.18	1.74	900	35.07	190(168)
$H_3S_{0.917}C_{0.083}$	$CS_{11}H_{36}$	$Pm\bar{3}m$	300	3.14	1.30	1353	30.29	168(151)
$H_3S_{0.9}C_{0.1}$	$CS_9H_{30}$	$C2/m$	230	3.26	1.80	1176	41.23	216(200)
$H_3S_{0.917}C_{0.083}$	$CS_{11}H_{36}$	$C2/m$	300	3.18	1.47	1338	35.30	189(172)
$H_3S_{0.9}C_{0.1}$	$CS_9H_{30}$	$C2/m$	180	3.12	1.84	1104	38.79	201(187)
$H_3S_{0.9}C_{0.1}$	$CS_9H_{30}$	$C2/m$	300	3.01	1.29	1429	31.17	169(153)

Despite performing thorough chemical composition and crystal structure searches for the C–S–H system at 300 GPa to tackle the unsolved puzzle of room-temperature superconducting carbonaceous sulfur hydride, neither a thermodynamically stable compound nor room-temperature superconductivity was identified. We have to mention that the validity of the experimental results has recently been questioned, where it has been proposed that either the measured superconductivity in C–S–H might be unconventional or the measurements might be erroneous. Clearly, more effort is required to fully understand the measured superconductivity in carbonaceous sulfur hydride.

#### 4. Conclusion

Extreme superhydrides represent a class of hydrogen-rich materials containing the highest atomic hydrogen content among binary metal hydrides reported to date. The structures of these MH<sub>18</sub> compounds consist of unique H<sub>36</sub> clathrate units stabilized under pressure starting around 300–400 GPa. Superconducting critical temperatures exceeding room temperature arise from favorable electronic density of states near the Fermi level and the large phonon energy scale of the vibration modes, as well as the strong electron–phonon coupling, as demonstrated for CeH<sub>18</sub> and ThH<sub>18</sub>. Meanwhile, other MH<sub>18</sub> compounds exhibit a wide range of  $T_c$  with variable combinations of electronic, phonon, and electron–phonon coupling. Recent focus in this research field has been mostly on reaching higher critical temperatures in ternary and higher multinary hydrides; the present work raises remarkable prospects that the bonding and electronic properties of the newly identified extreme binary superhydrides parallel those of

atomic metallic hydrogen, giving rise to the highest  $T_c$  values among all known thermodynamically stable superhydrides. Furthermore, we have examined the influence of various heavy elements in hydrogen-rich

superconductors over a range of pressures, and the resulting insights extend and refine the original conjecture of reducing the pressure for achieving AMH-like superconductivity by chemical doping and chemical precompression. Additional considerations of electron<sup>-31</sup> or hole<sup>-47</sup>doping effects in these extreme superhydrides may provide a promising platform for further exploration and optimization of superconductors that may host extraordinary above-room-temperature superconductivity.

In addition, we have extensively explored the phase space of carbonaceous sulfur hydrides at 300 GPa by using the CALYPSO structure prediction and cluster expansion method. Although no thermodynamically stable phase was found, several metastable crystals have been identified to be high-temperature superconductors with  $T_c$  values of 100–200 K. The coordination number of the C and S atoms in H-rich metastable C–S–H crystals are four and six, respectively, with the formation of CH<sub>4</sub> and SH<sub>6</sub> units, where the remaining H atoms form H<sub>2</sub> units in pairs. Such kinds of molecular crystals are apparently not good candidates for room-temperature superconductors. Using primitive cells up to 64 atoms,  $T_c$  values of H<sub>3</sub>S-like structures with low levels of carbon doping were estimated to be ~189 K for H<sub>3</sub>S<sub>0.917</sub>C<sub>0.083</sub> at 300 GPa, for the reason that doping localizes electrons in C–H bonds and then decreases the  $N(E_F)$ . Our current results provide a comprehensive map between the crystal structure and superconductivity of carbonaceous sulfur hydride materials at high pressures. More efforts, both theoretically and experimentally, are required to be done for making the mechanism of room-temperature superconducting in carbonaceous sulfur hydride clear.

#### 5. Schedule and prospect for the future

I have been a HOKUSAI general user and wish to continue using the system. During the last fiscal year 2022, I have finished work on RE-H and C-S-H

## Usage Report for Fiscal Year 2022

compounds, and have published two articles on JACS and PRB, respectively. For the next fiscal year, we plan to continue using the HOKUSAI supercomputer to study the stability and superconductivity of compressed superhydrides, where new high-temperature superconductors and even room-temperature superconductors are expected to be proposed. We expect high-standard publications can be eventually achieved.

6. If no job was executed, specify the reason.

Usage Report for Fiscal Year 2022

**Fiscal Year 2022 List of Publications Resulting from the Use of the supercomputer**

**[Paper accepted by a journal]**

X. Zhong, Y. Sun, T. Iitaka, M. Xu, H. Liu, R. J. Hemley, C. Chen, and Y. Ma, *Prediction of Above-Room-Temperature Superconductivity in Lanthanide/Actinide Extreme Superhydrides*, *J Am Chem Soc* **144**, 13394 (2022).

Y. Sun, X. Li, T. Iitaka, H. Liu, and Y. Xie, *Crystal Structures and Superconductivity of Carbonaceous Sulfur Hydrides at Pressures up to 300 GPa*, *Phys Rev B* **105**, 134501 (2022).

**[Conference Proceedings]**

**[Oral presentation]**

**[Poster presentation]**

**[Others (Book, Press release, etc.)]**