

# Application of GPU computation toward particle physics

Eigo Shintani (RIKEN-BNL)

# Overview

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- ▶ Introduction
- ▶ Precision physics in the particle physics
  - ▶ Muon  $g-2$
  - ▶ Nucleon EDM
  - ▶ Proton decay
- ▶ Application of GPU
  - ▶ Status of lattice QCD calculation
  - ▶ Perspectives
- ▶ Summary

Introduction:

# Grand challenges

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Can we understand the origin of nature ?



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Need deeply understanding of three frontier



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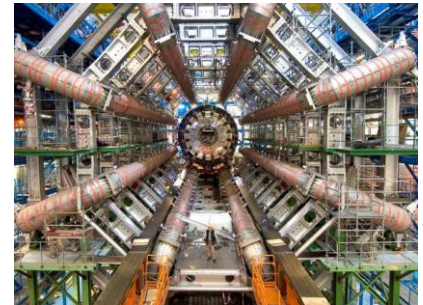
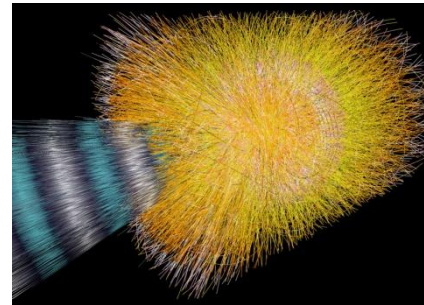
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Analysis of  $O(10^{10})$  events



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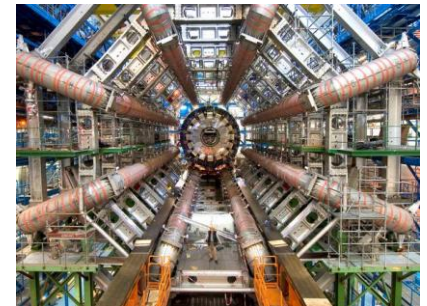
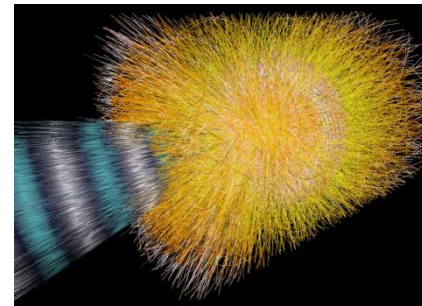
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Sensitive detector (Kamioka, ...),  
Detect a rare event  
in  $O(10^{-10})$  probability

Putting it all together...

$$a_{\mu}^{\text{exp}} = 116\,592\,089\,(63) \times 10^{-11}$$

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$$a_{\mu} = \frac{g-2}{2}$$



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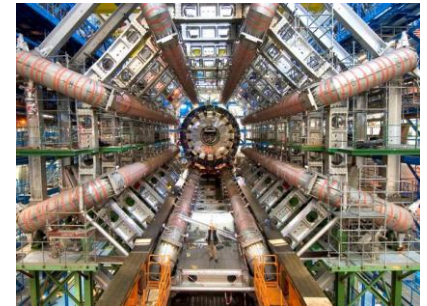
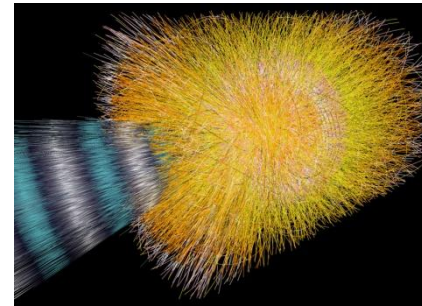
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- **Cosmic frontier**

Look up the sky carefully !



# Introduction:

# What has been interesting so far ?

## ► Making comprehensive list of fund. particles

Three Generations of Matter (Fermions)

	I	II	III	
mass→	3 MeV	1.24 GeV	172.5 GeV	0
charge→	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0
spin→	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
name→	<b>u</b> up	<b>c</b> charm	<b>t</b> top	<b>γ</b> photon
Quarks	6 MeV	95 MeV	4.2 GeV	0
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	0
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
	<b>d</b> down	<b>s</b> strange	<b>b</b> bottom	<b>g</b> gluon
Leptons	<2 eV	<0.19 MeV	<18.2 MeV	90.2 GeV
	0	0	0	0
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
	<b>ν<sub>e</sub></b> electron neutrino	<b>ν<sub>μ</sub></b> muon neutrino	<b>ν<sub>τ</sub></b> tau neutrino	<b>Z<sup>0</sup></b> weak force
	0.511 MeV	106 MeV	1.78 GeV	80.4 GeV
	-1	-1	-1	$\pm 1$
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
	<b>e</b> electron	<b>μ</b> muon	<b>τ</b> tau	<b>W<sup>±</sup></b> weak force

- Established in the experiment

### Quarks (3 generations)

u, d, s, c, b, t

### Leptons (3 generations)

electron, muon, tau, and neutrino

### Bosons

γ, g, Z, W (spin-1)

- Almost established in LHC

Higgs (spin-0) → discovery is very soon ?

- Not yet

Graviton (spin-2)

## Theory:

Standard Model (QED, QCD, EW)



Introduction:

# Quantum chromodynamics

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- ▶ Treating *the fascinating problems* in hadron physics
  - ▶ How is the constitution of  $O(100)$  hadrons with 12 quarks ?
  - ▶ Why quarks (and gluon) are not directly visible ?
  - ▶ Why meson mass is so different ( $\pi \sim 135\text{MeV}$ ,  $\eta' \sim 960\text{MeV}$ ) ?
  - ▶ Why quark has fractional charge ?

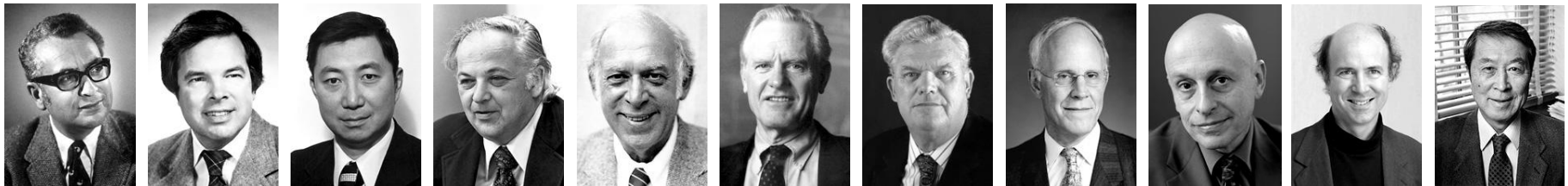
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- ▶ **QCD provides the *smart solutions* (asymptotic freedom, spontaneous sym. breaking, anomaly, ...) using *very simple formula***

$$\mathcal{L} = \sum_q \bar{\psi}_{q,a} (i\gamma^\mu \partial_\mu \delta_{ab} - g_s \gamma^\mu t_{ab}^C \mathcal{A}_\mu^C - m_q \delta_{ab}) \psi_{q,b} - \frac{1}{4} F_{\mu\nu}^A F^{A\mu\nu}$$

*This is one of the most successful theory beyond perturbation !*



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  - ▶ LHC era ( $> 10$  TeV) might be *the oasis* of new particle.
  - ▶ Remaining the unexplained issues by the SM
    - ▶ Why neutrino has mass ?
    - ▶ Why **T(time-reversal)-violation** in QCD and BSM is so small ?
    - ▶ Why proton does not decay ?
    - ▶ ...

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These problems have not been clear due to extremely tiny signal ( $\langle O \rangle < 10^{-10}$ , less than single precision )

⇒ need to the precision physics

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Precision physics:

# What is going on?

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- How long lifetime of proton ?

- Maybe more than  $10^{33}$  year ...

- (if not decay, where did we come from ?)

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QCD (hadron) effect is important  
for these observables !

Some aspects from *effective models* but it has not been solid statement.  
To know *hadron effect* exactly, we should deal with non-perturbative method.

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# Muon $g-2$

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► The extremely precise measurement

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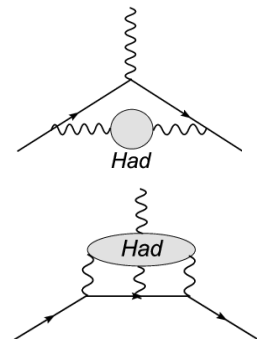
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▶ Main uncertainties in the SM

- Leading order of hadronic contribution (HVP);  
~90% of error
- Next-to-leading order of hadronic contribution (light-by-light);  
~ *unknown*, may be large uncertainty



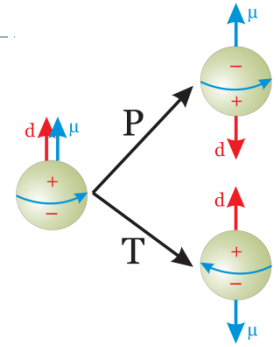
Need to precisely calculate HVP and LbyL, being independent from models.

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# Nucleon EDM

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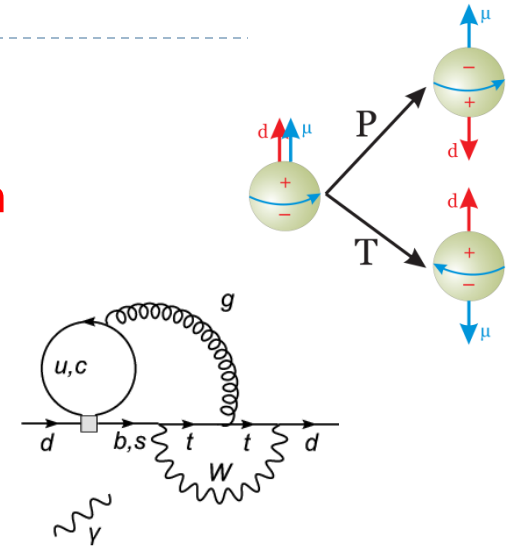
but this is almost zero; **upper limit:  $< 2.9 \times 10^{-26} \text{ e} \cdot \text{cm}$**





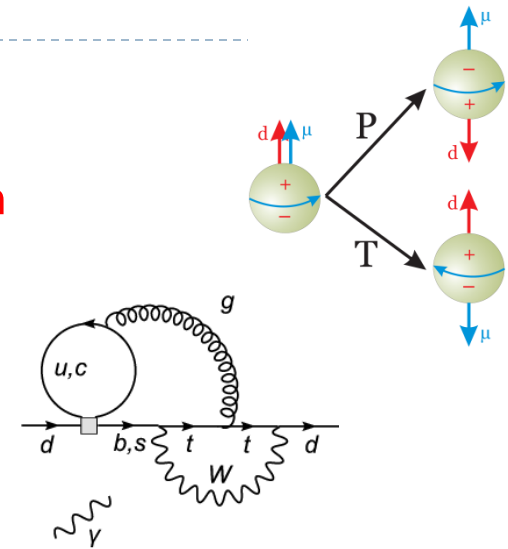
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- ▶ **Contribution from weak boson: CKM phase**  
Very **tiny**, which is 3-loop :  $d_N^{\text{KM}} \simeq 10^{-30} \text{ -- } 10^{-32} \text{ e} \cdot \text{cm}$   
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- ▶ Contribution from QCD:  $\theta$  term  
**Unnaturally small (strong CP problem)  $\bar{\theta} < 10^{-9 \pm 1}$**



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- ▶ Contribution from BSM: dim-5,6 operator

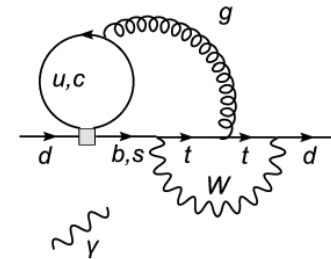
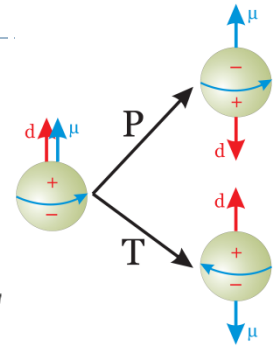
$$\mathcal{O}_{q\text{EDM}} = d_q \bar{q}(\sigma \cdot F)\gamma_5 q, \quad \mathcal{O}_{c\text{EDM}} = d_q^c \bar{q}(\sigma \cdot G)\gamma_5 q$$

$$d_N = d_N^{\text{QCD}} \bar{\theta} + d_N(d_q, d_q^c) + d_N(d^G)$$

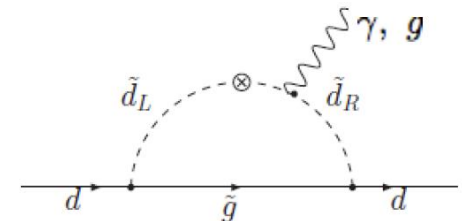
$$\sim 10^{-17} [\text{e} \cdot \text{cm}] \bar{\theta} + (1.4 - 0.47) d_d - (0.12 - 0.35) d_u + O(10^{-2}) d_q^c$$

$$\sim O(10^{-25} - 10^{-27}) \text{ e} \cdot \text{cm}$$

→ Close to the bound of experiment



Crewther, et al. (1979),  
Ellis, Gaillard (1979)



Hisano, Shimizu (04), Ellis, Lee, Pilaftsis (08),  
Hisano, Lee, Nagata, Shimizu (12)

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# Proton decay

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- ▶ **Smoking gun of Grand Unified Theories (GUTs)**
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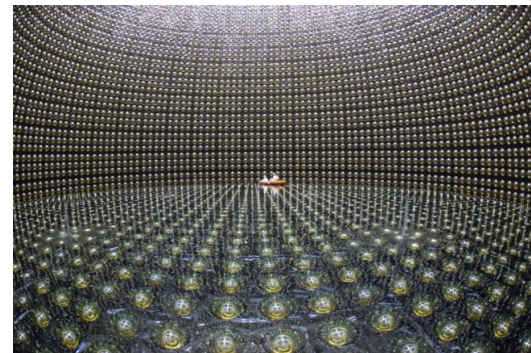
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- ▶ Experiments

- ▶ Super-Kamiokande leads to bound:

$$\tau(p \rightarrow e^+ \pi^0) > 8.2 \times 10^{33} \text{ years}$$

Nishino et al. (Super-Kamiokande), PRD85, 112001 (2012)

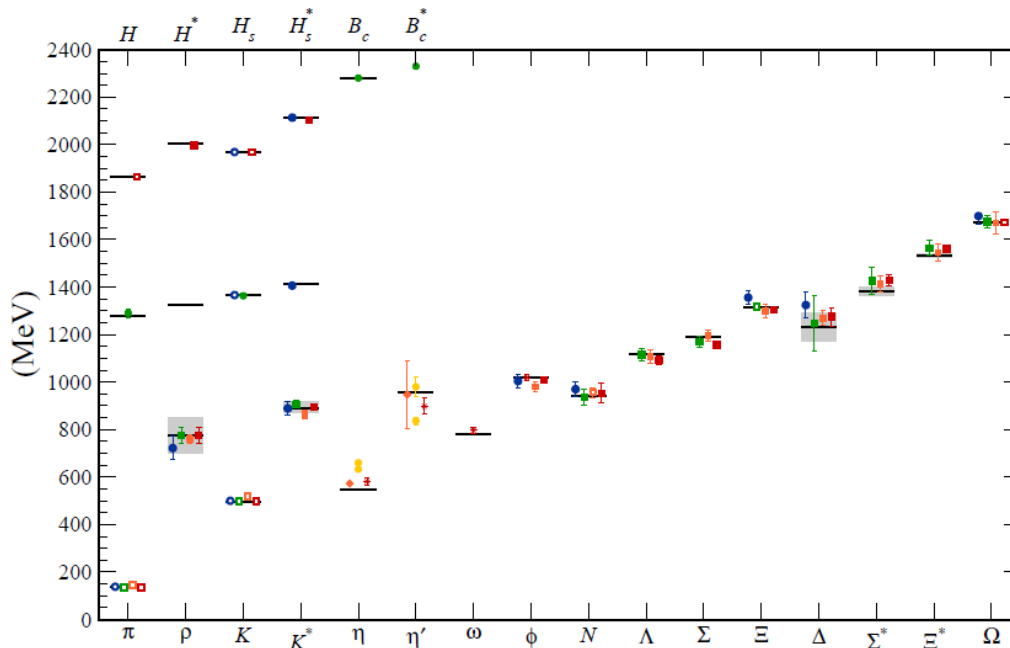
We should make sure whether GUTs are excluded or not ?





# Precision physics: Lattice QCD

- ▶ **Appropriate tool to precisely investigate hadron effect**
  - ▶ Enable us to evaluate hadron contribution in the particle physics.
  - ▶ Elegant methodology
    - ▶ Gauge symmetry and renormalizability
    - ▶ A few input parameters (cut-off scale, and quark mass)



Lattice QCD provides almost consistent values of hadron spectroscopy, including heavy quarks, with experiment.

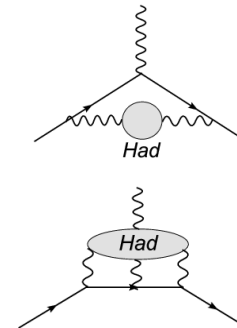
Kronfeld, I209.3468

# Status & Perspectives

## ▶ Lattice calculation in $N_f = 2+1$ DWFs

### ▶ Muon $g-2$

- ▶ Leading order hadron contribution:  
10% accuracy → a few % required
- ▶ The next-to-leading order :  
unknown → around 10% accuracy



### ▶ Nucleon EDM

- ▶ Recently we have 30 % precision (stat.) of nucleon EDM.
- ▶ To establish it, we require less than 10 % total error.

### ▶ Proton decay

- ▶ Recent result shows that  $p \rightarrow \pi$  channel has 30% total error.
- ▶ It is possible to reduce the error to around a few %. Aoki, ES, Soni, 1304.7424

Note : these are estimate using AMA algorithm ( $\times 5$  faster).

# Error reduction techniques

## ▶ Covariant approximation averaging (CAA)

- ▶ For original observables  $O$ , (unbiased) improved estimator

$$\mathcal{O}^{(\text{imp})} = \mathcal{O}^{(\text{rest})} + \frac{1}{N_G} \sum_{g \in G} \mathcal{O}^{(\text{appx}),g}, \quad \mathcal{O}^{(\text{rest})} = \mathcal{O} - \mathcal{O}^{(\text{appx})}$$

which satisfies  $\langle O \rangle = \langle O^{\text{imp}} \rangle$  if approximation is **covariant under lattice symmetry  $g$** , and error becomes  $\text{err}^{\text{imp}} \simeq \text{err} / \sqrt{N_G}$

## ▶ All-mode averaging (AMA)

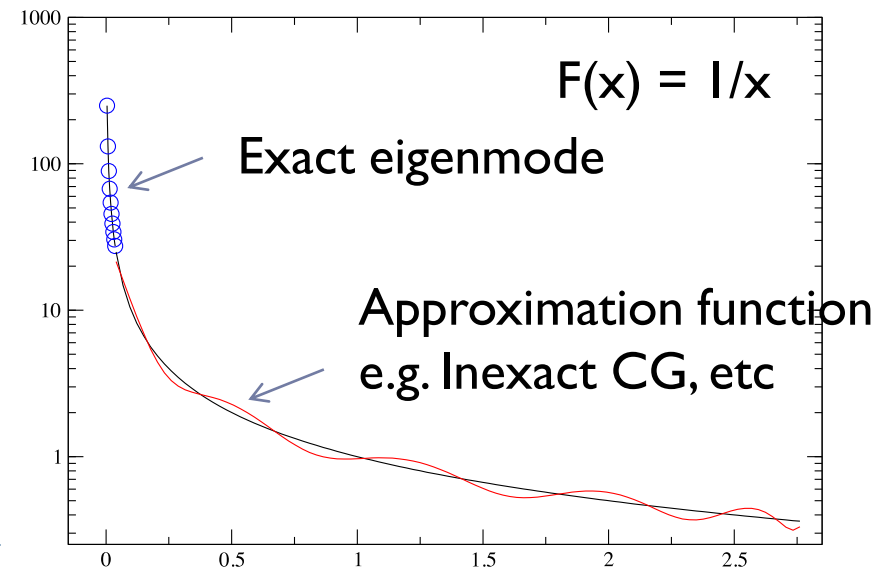
$$\mathcal{O}^{(\text{appx})} = \mathcal{O}[S_l],$$

$$S_l = \sum_{\lambda} v_{\lambda} F(\lambda) v_{\lambda}^{\dagger},$$

$$F(\lambda) = \begin{cases} \lambda^{-1}, & |\lambda| < \lambda_{\text{cut}} \\ P_n(\lambda) \simeq \lambda^{-1} & |\lambda| > \lambda_{\text{cut}} \end{cases}$$

accuracy control :

- low mode part : # of eig-mode
- mid-high mode : degree of poly.



# GPU accelerator of lattice QCD

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- ▶ GPU computation becomes the big stream in lattice QCD
  - ▶ Reasonable cost-performance and potential of improvement
  - ▶ Alternative resource to CPU cluster
  - ▶ Take advantage of fast implementation of CG inverter
  - ▶ Interesting applications (*for me*)
    - ▶ HMC applications
      - There have been many trials using staggered fermion or Wilson fermion.
    - ▶ Fast implementation of Dirac inverter as preconditioner
      - Mixed precision seems to be efficient. Mike's and Hyung-Jin's talk
    - ▶ Computation of eigenmode of Dirac matrix
      - Important, but huge memory size might be bottom neck.
    - ▶ Application to stochastic method

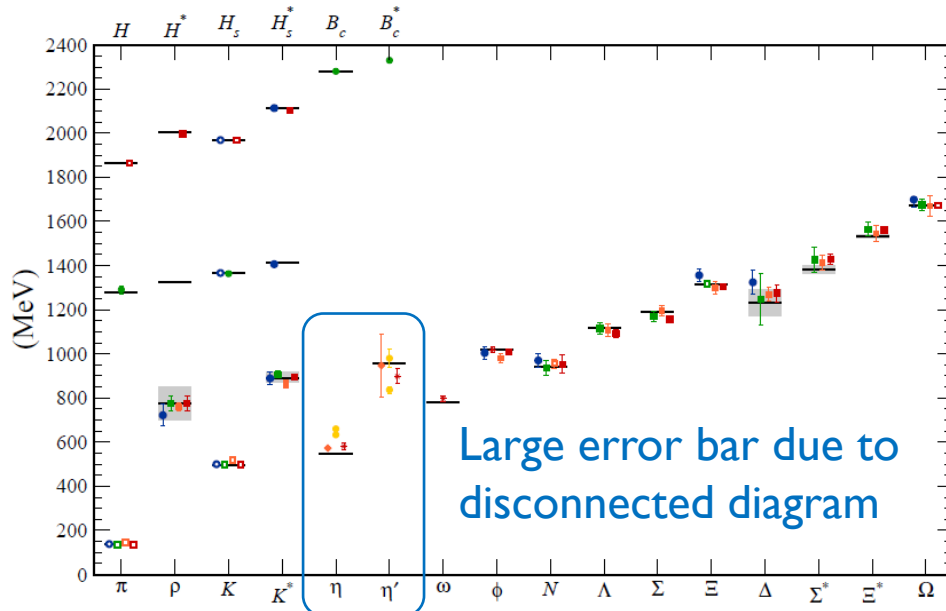
# Application of GPU:

## Example

### ▶ Disconnected diagram

- ▶ *can of the worm*
- ▶ Computation of trace of the matrix inverse using stochastic method:

$$\text{Tr } D^{-1}(x, x) \simeq N^{-1} \sum_i \eta_i^\dagger(x) D^{-1}(x, y) \eta_i(y), \quad \eta_i(x) = e^{i\xi_i(x)} \quad \xi_i : \text{random number from } [0:2\pi)$$



- This is based on approximation
 
$$\delta_{x,y} \simeq \sum_i \eta_i^\dagger(x) \eta_i(y) / N$$
- Additional CG iteration of noise number is needed ( $\times O(100)$ )
- **Disconnected diagram has rich info. of isospin breaking etc.**

Fast CG algorithm or preconditioning is very useful.

# Study of lattice QCD with GPU

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## ▶ There are several publications

### Testing HMC with staggered fermion

- Egri, et al., “Lattice QCD as a video game”, *Comput.Phys.Commun.* 177,631 (2007).
- Bonati et al.”QCD simulations with staggered fermion on GPUs”, *Comput.Phys.Commun.* 183,853 (2012).

### Study of finite temperature

- Aoki et al.,” The QCD transition temperature: results with physical masses in the continuum limit II”, *JHEP* 0906 (2009) 088.
- Endrodi et al., “The QCD phase diagram at nonzero quark density”, *JHEP* 1104 (2011) 001.

### Algorithm with mixed precision

- Clark, et al.,”Solving Lattice QCD systems of equations using mixed precision solvers on GPUs”, *Comupt.Phys.Commun.* 181,1517(2010).
- Babich, et al.,”Scaling Lattice QCD beyond 100 GPUs”, arXiv: 1109.2935
- Jang, et al. “Multi GPU Performance of Conjugate Gradient Solver with Staggered fermions in Mixed Precision”, arXiv: 1111.0125

# Request from precision physics

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- ▶ Domain-Wall fermion (DWF) is important to control the systematic error of lattice artifacts.
- ▶ Now preparing the gauge configurations including physical quarks in 5 fm volume. RBC/UKQCD collaboration
- ▶ Target simulation size:
  - ▶  $48^3 \times 96 \times 16$  lattice in physical pion mass :  $m_\pi = 135$  MeV
  - ▶ >200 eigenmodes of even-odd DWF kernel
  - ▶ Required performance:  
Memory ~ 4 TB, Flops > 40TFlops/job  
→ excellent scalability is needed (as well as Blue Gene series ...)

# Summary

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- ▶ Particle physics is being precision physics.
- ▶ Reliable calculation in the SM plays an essential role to proceed to BSM search.
- ▶ Lattice QCD is the most appropriate.
- ▶ To confirm the SM prediction for **muon  $g-2$ , nucleon EDM and proton decay**, GPU computation is helpful.
- ▶ We have to search the best way for the implementation:
  - ▶ Mixed precision ?
  - ▶ Hybrid with CPU ?
- ▶ Expect GPU has a lot of potential.



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Thank you for your attention !

